

(Research Article)

Chaotic Algorithm for Solving Optimal Reactive Power Problem

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Abstract

In this work Chaotic Krill Herd (CKH) algorithm is utilized to solve the optimal reactive power problem. Herd behaviour deeds of the Krill individuals are imitated to formulate the algorithm. Key task for the Krill movement is the least distance of each individual Krill from food to the maximum concentration of the herd. Based on the persuaded movement of other Krill's, foraging movement and substantial propagation the location of every krill in a time period is depended. Chaos theory and the logistic chaotic mapping are used in substantial propagation to improve the search ability of the proposed algorithm. Proposed Chaotic Krill Herd (CKH) algorithm has been validated in IEEE 57, 300 test systems. Real Power Loss is reduced considerably when compared to other standard algorithms.

Keywords: Optimal Reactive Power, Transmission loss, optimization, Chaotic Krill Herd

1. Introduction

In power system operation & control, reactive power problem plays the key role in secure & economic operation of the power system. Several conventional methods [1-6] used already for solving the problem. But many drawbacks have been found in the conventional methods and mainly difficulty in handling the inequality constraints. Last two decades many evolutionary algorithms [7-17]. In this work Chaotic Krill Herd algorithm is utilized to solve the optimal reactive power problem. Herd behaviour deeds of the Krill individuals are imitated to formulate the algorithm. Key task for the Krill movement is the least distance of each individual Krill from food to the maximum concentration of the herd. Based on the persuaded movement of other Krill's, foraging movement and substantial propagation the location of every krill in a time period is depended. The symphony of the krill herd after predation depends on many parameters. The herding of the krill individuals has two key goals: swelling of krill concentration, and accomplishment of food. Depth of grouping the krill (mounting concentration) and finding food (region of elevated food concentration) are used as objectives which ultimately direct the krill herd approximately the global minimum. In this process, an individual krill budge toward the most excellent solution when it explore for the uppermost concentration and food. Progression persuaded by other krill individuals by Foraging action and arbitrary propagation. Chaos theory and the logistic chaotic mapping are used in substantial propagation to improve the search

ability of the proposed algorithm. Proposed Chaotic Krill Herd (CKH) algorithm has been validated in IEEE 57, 300 test systems. Real Power Loss is reduced considerably when compared to other standard algorithms.

2. Problem Formulation

Main aim is to minimize the system real power loss & given as,

$$P_{loss} = \sum_{k=1}^n \sum_{(i,j)} g_k (V_i^2 + V_j^2 - 2V_i V_j \cos \theta_{ij}) \quad (1)$$

PL – power loss, g_k – conductance of branch, V_i and V_j are voltages at buses i, j , Nbr – total number of transmission lines in power systems.

Voltage deviation magnitudes (VD) is,

$$\text{Min (VD)} = \sum_{k=1}^n |V_k - 1.00| \quad (2)$$

Load flow equality constraints:

$$P_{Gi} - P_{Di} - V_i \sum_{j=1}^{nb} V_j \begin{bmatrix} G_{ij} & \cos \theta_{ij} \\ +B_{ij} & \sin \theta_{ij} \end{bmatrix} = 0, i = 1, 2, \dots, nb \quad (3)$$

$$Q_{Gi} - Q_{Di} - V_i \sum_{j=1}^{nb} V_j \begin{bmatrix} G_{ij} & \sin \theta_{ij} \\ +B_{ij} & \cos \theta_{ij} \end{bmatrix} = 0, i = 1, 2, \dots, nb \quad (4)$$

active power of slack bus is symbolized by P_G and reactive power of generators symbolized by Q_G

Inequality constraints are:

Upper and lower bounds on the bus voltage magnitudes (V_i) is given by:

$$V_{Gi}^{\min} \leq V_{Gi} \leq V_{Gi}^{\max}, i \in ng \quad (5)$$

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$$V_{Li}^{\min} \leq V_{Li} \leq V_{Li}^{\max}, i \in nl \quad (6)$$

Upper and lower bounds on the compensators (Qc) is given by:

$$Q_{Ci}^{\min} \leq Q_{Ci} \leq Q_{Ci}^{\max}, i \in nc \quad (7)$$

$$Q_{Gi}^{\min} \leq Q_{Gi} \leq Q_{Gi}^{\max}, i \in ng \quad (8)$$

Upper and lower bounds on the transformers tap ratios (Ti) are given by:

$$T_i^{\min} \leq T_i \leq T_i^{\max}, i \in nt \quad (9)$$

$$S_{Li}^{\min} \leq S_{Li}^{\max}, i \in nl \quad (10)$$

3. Krill herd algorithm

Krill has capability of forming huge swarms. Systematic deeds of krill have been imitated to form the algorithm. The krill individuals try to preserve an elevated concentration and budge due to their shared effects [18]. Itinerary of motion persuade, α_i , and is computed from the local swarm concentration (confined outcome), a target swarm concentration (attack outcome), and a repulsive swarm concentration (hideous outcome).

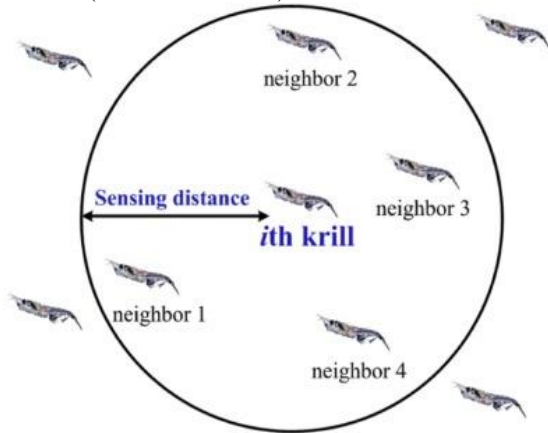


Figure 1. Krill position

Krill's individual movement can be defined as:

$$P_i^{\text{new}} = P^{\text{max}} \alpha_i + \omega_n P_i^{\text{old}} \quad (11)$$

Where

$$\alpha_i = \alpha_i^{\text{confined}} + \alpha_i^{\text{attack}} \quad (12)$$

P_i^{new} - new movement of krill, P^{max} - maximum movement of krill, ω_n - inertia weight, $\alpha_i^{\text{confined}}$ - effect provided by neighbours, α_i^{attack} - direction provided by best krill

Individual krill movement based on the outcome of the neighbours is defined by:

$$\alpha_i^{\text{confined}} = \sum_{j=1}^{pp} \bar{K}H_{ij} \hat{Z}_{ij} \quad (13)$$

$$\hat{Z}_{ij} = \frac{z_j - z_i}{\|z_j - z_i\| + \epsilon} \quad (14)$$

$$\bar{K}H_{ij} = \frac{KH_i - KH_j}{KH^{\text{poor}} - KH^{\text{good}}} \quad (15)$$

\hat{Z}_{ij} - relative positions, $\bar{K}H_{ij}$ - fitness of the krill herd

Each krill individual sensing distance can be found for every iteration:

$$DS_{s,i} = \frac{1}{EN} \sum_{j=1}^N \|Z_i - Z_j\| \quad (16)$$

$DS_{s,i}$ - sensing distance of the krill

Most excellent fitness of individual krill is taken into account by,

$$\alpha_i^{\text{attack}} = CF^{\text{good}} \bar{K}H_{i,\text{good}} \hat{Z}_{i,\text{good}} \quad (17)$$

CF^{good} - effect of the coefficient of the krill

CF^{good} is defined as:

$$CF^{\text{good}} = 2 \left(\text{random} + \frac{i}{i_{\text{maximum}}} \right) \quad (18)$$

For the i th krill individual the Foraging motion can be articulated by,

$$Fg_i = vl_f \beta_i + \omega_f Fg_i^{\text{old}} \quad (19)$$

Where

$$\beta_i = \beta_i^{\text{food}} + \beta_i^{\text{good}} \quad (20)$$

vl_f - foraging speed, ω_f - inertia weight, Fg_i - last foraging motion, β_i^{food} - food attractive

For every iteration the centre of food is created by,

$$Z^{\text{food}} = \frac{\sum_{i=1}^F \frac{1}{K_i} Z_i}{\sum_{i=1}^F \frac{1}{KH_i}} \quad (21)$$

for the i th krill individual food attraction is given as:

$$\beta_i^{\text{food}} = CF^{\text{food}} \bar{K}H_{i,\text{food}} \hat{Z}_{i,\text{food}} \quad (22)$$

The food coefficient is defined by,

$$CF^{\text{food}} = 2 \left(1 - \frac{i}{i_{\text{maximum}}} \right) \quad (23)$$

Most excellent fitness of the i th krill individual is found by:

$$\beta_i^{\text{best}} = \bar{K}H_{i,\text{good}} \hat{Z}_{i,\text{good}} \quad (24)$$

The physical dissemination, utmost dissemination speed is formulated as follows:

$$DS_i = DS^{maximum} \delta \quad (25)$$

On the basis of a geometrical annealing sketch out, it can be formulated as:

$$DS_i = D^{maximum} \left(1 - \frac{I}{I_{maximum}}\right) \delta \quad (26)$$

Position vector of a krill individual during the interval t to $t + \Delta t$ is given by,

$$Z_i(t + \Delta t) = Z_i(t) + \Delta t \frac{dZ_i}{dt} \quad (27)$$

Δt Entirely depends on the search space and it obtained from the following,

$$\Delta t = CF_t \sum_{j=1}^{PV} (UB_j - LB_j) \quad (28)$$

Genetic reproduction mechanisms are integrated into the Krill herd algorithm to improve the performance of the algorithm.

a. Crossover

$$Z_{i,m} = \begin{cases} Z_{r,m} & \text{random}_{i,m} < Cr \\ Z_{i,m} & \text{else} \end{cases} \quad (29)$$

$$Cr = 0.210 \bar{KH}_{i,best} \quad (30)$$

b. Mutation

$$Z_{i,m} = \begin{cases} Z_{gbes,m} + \mu(Z_{p,m} - Z_{q,m}) & \text{random}_{i,m} < Mu \\ Z_{i,m} & \text{else} \end{cases} \quad (31)$$

$$Mu = 0.0475 / \bar{KH}_{i,best} \quad (32)$$

- Initialization of population.
- Fitness assessment of each krill individual based on its location.
- Motion calculation:
Motion induced by the attendance of other individuals,
Foraging movement
Physical propagation
- Applying the genetic operators
- Updating krill individual location in the search space.
- until the stop criteria is reached; Replicate: go to step fitness evaluation
- End

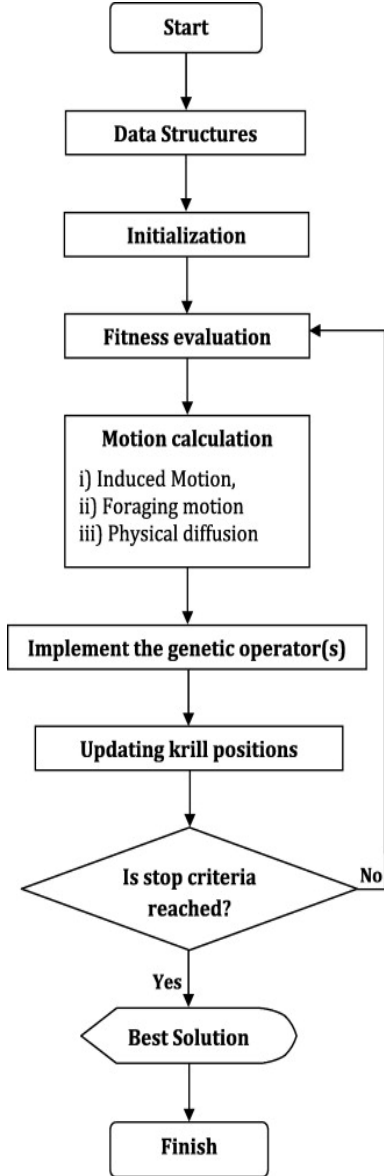


Figure 2. Flowchart for krill herd algorithm

4. Chaotic Krill Algorithm

Chaos is a trend that is known as a progress in controlled amplitude which has been happen in a specific vibrant non-linear system [19]. Intriguing into relation of eminent sensitivity of the chaotic functions in the direction of the most important conditions, broad diversity in this sequence are occurred so that no reappear elements are isolated through the population. In order to generate a logistic chaotic portrait a polynomial quadratic portrait which is mentioned below has been applied:

$$y(i + 1) = \mu y(i) \cdot (1 - y(i)), y(i) \in [0,1], i = 1 \sim n \quad (33)$$

$y(i)$ in this equation is the magnitude of the x in the “ i ” th step, and is known control parameter for the system. If μ is between 3 and 4 it reveals the chaotic behaviour of the function. In this work μ is assumed to be equal to 4.

- a. Initialization of population.
- b. Fitness assessment of each krill individual based on its location.
- c. Motion calculation:
 Motion induced by the attendance of other individuals,
 Foraging movement
 Physical propagation
 Corporeal propagation pedestal on chaotic sketch
- d. Applying the genetic operators
- e. Updating krill individual location in the search space.
- f. until the stop criteria is reached; Replicate: go to step fitness evaluation
- g. End

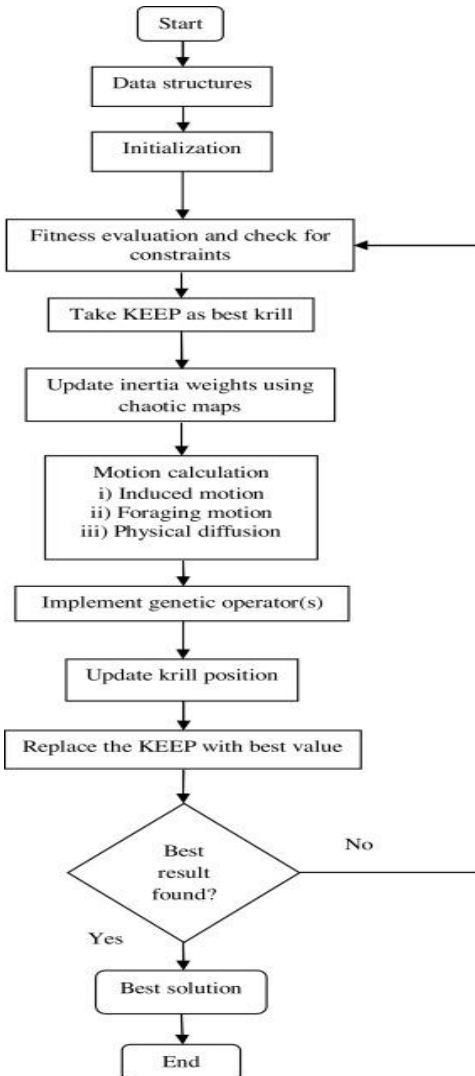


Figure.3. Flow chart for chaotic based krill heard algorithm

5. Simulation Results

At first IEEE 57 bus system [20] is used as test system to validate the performance of the proposed Chaotic Krill Herd (CKH) algorithm. Total active and reactive power demands in the system are 1248.23 MW and 334.16 MVAR, respectively. Generator data the system is given in Table 1. The optimum loss comparison is presented in Table 2. Figure 4 gives the comparison of active power loss

Table 1. Generator limits

Generator No	Pgi minimum	Pgi maximum	Qgi minimum	Qgi maximum
1	25.00	50.00	0.00	0.00
2	15.00	90.00	-17.00	50.00
3	10.00	500.00	-10.00	60.00
4	10.00	50.00	-8.00	25.00
5	12.00	50.00	-140.00	200.00
6	10.00	360.00	-3.00	9.00
7	50.00	550.00	-50.00	155.00

Table 2. Comparison of Losses

Parameter	CLPSO [16]	DE [15]	GS A [15]	OG SA [17]	SO A [16]	QO DE [15]	CS A [21]	CKH
PLOSS (MW)	24.5152	16.7857	23.4611	23.43	24.2654	15.8473	15.5149	13.5010

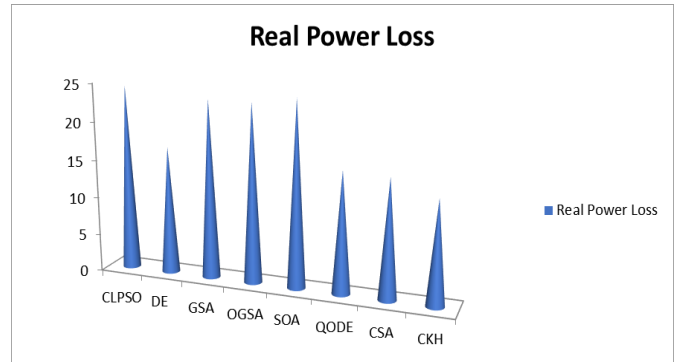


Figure 4. Comparison of active power loss

Secondly IEEE 300 bus system [15] is used as test system to authenticate the performance of the proposed Chaotic Krill Herd (CKH) algorithm. Table 3 shows the comparison of real power loss obtained after optimization. Fig 5 gives the comparison of real power loss

Table 3 Comparison of Real Power Loss

Parameter	EGA [22]	EEA [22]	CSA [21]	CKH
PLOSS (MW)	646.2998	650.6027	635.8942	626.0478

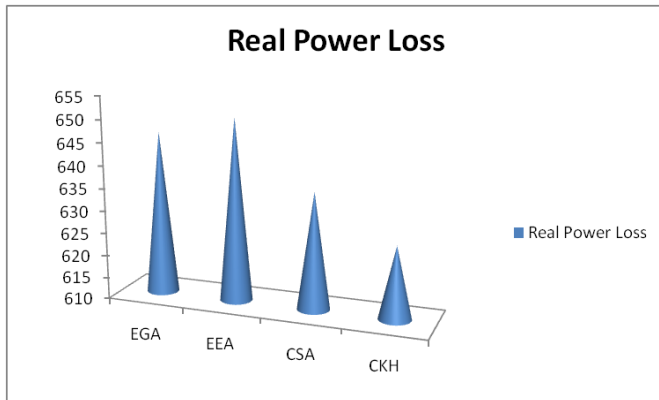


Figure 5. Real power loss comparison

6. Conclusion

In this paper Chaotic Krill Herd (CKH) algorithm is successfully solved the optimal reactive power problem. Real Power Loss is reduced considerably when compared to other standard algorithms. Chaos theory and the logistic chaotic mapping are used in substantial propagation to improve the search ability of the proposed algorithm. Proposed Chaotic Krill Herd (CKH) algorithm has been validated in IEEE 57, 300 test systems. Real Power Loss is reduced considerably when compared to other standard algorithms.

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Biographical notes



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